

# Fuzzy-Logic Modeling Approach for System Requirements Management

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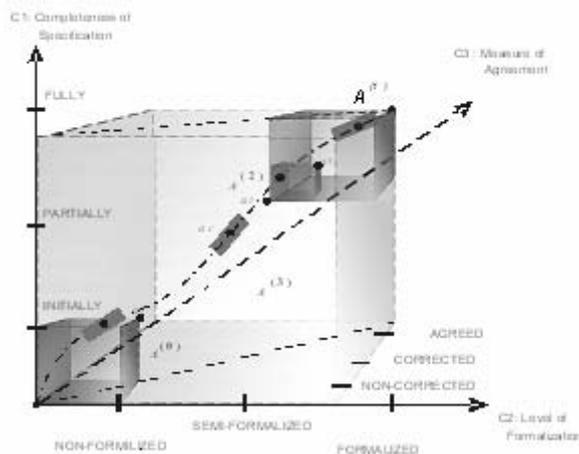
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Based on the concept of multi-dimensional information space presented in [TSM04], we propose to consider so-called *state space* for system requirements (SR) called further as  *$\Pi$ -space*. The dimensions of  $\Pi$  should describe a current state of a SR for any application domain in some *problem-independent* and *unified* manner. In order to establish such a description for any SR, the following three criteria are introduced, namely: *C1-Completeness of Specification*, it defines the degree of requirements completeness in some project; *C2 - Level of Formalization*, it indicates the formalizing degree of given SR; *C3 - Measure of Agreement*, it shows to which degree the stakeholders (domain experts, analysts, programmers, etc.) are agreed from their points of view to SR in project considered. These criteria C1-C3 are really complex and weakly formalized. Basically, the criteria values C1-C3 are *orthogonal logically* because some project's state is possible, when there is the completed functional description of given SR (it means  $C1=C1_{\max}$ ), but the level of it's formalization is low ( $C2=C2_{\min}$ ), and in addition to this the measure of coordination is also very poor (i.e.,  $C3=C3_{\min}$ ); in the same way all others logical combinations of criteria values C1-C3 could be constructed, etc. If criteria values of C1-C3 are fuzzy defined, the  $\Pi$ -space is the fuzzy set, and it could be defined as subset from Cartesian product of those fuzzy sets, namely:  $\Pi \subseteq D(C1) \times D(C2) \times D(C3)$  where:  $D(C_i), i \in [1,3]$  - is a fuzzy set (a values domain) of the appropriate criteria. Furthermore, because of the criteria *C3: Measure of Consistency*, each point in the  $\Pi$ -space represents some *alternative estimation* (further - *an alternative*) for a given SR: a value  $a_i$ . We describe the criteria C1-C3 using *linguistic variables* (LV), which are defined in fuzzy set  $\Pi$ . In this way the new subspace  $A \subseteq C1 \times C2 \times C3$  is constructed into the  $\Pi$  -space, and at that  $A \subset \Pi$ . Taking into account some empirical considerations about SR alternative values in a design process, there are 4 *different areas* in subspace A which correspond to appropriate alternative

values for some SR  $a_i \in A$ , namely:  $A^{(0)} \subset A$  is the area of *initial (or non-defined)* alternatives;  $A^{(1)}$  is the area of *well-defined alternatives*, at that  $A^{(1)} \cap A^{(0)} = \emptyset$ ;  $A^{(2)}$  is the area of *effectively alternatives*, at that  $(A^{(2)} \subset A^{(1)})$  and  $A^{(2)} \neq \emptyset$ ;  $A^{(3)} = A \setminus (A^{(0)} \cup A^{(1)})$  is the area of *weakly-defined alternatives*. Here the following rules for main possible kinds of SR-alternatives (SRA)  $a_i$  are introduced, namely: (1) if some  $a_i \in A^{(0)}$  then it is not possible to have *running* SWS based on its description given in the criteria values C1-C3; (2) if some  $a_i \in A^{(1)}$  then it is possible, based on its description, to perform some design procedures and to create *an efficient* SWS; (3) if some  $a_i \in A^{(2)}$  then it is possible, based on its description, to perform some design procedures and to gain *an efficient enough* SWS, i.e. some SWS having an efficient level not less some pre-defined value; (4) if some  $a_i \in A^{(3)}$  then based on this SR an appropriate SWS could be found with some *degree of risk* only (this is so-called area of *unstable designing* into the subspace A). Taking into account these definitions, we propose the graphical representation for the subspace A as depicted on Fig. 1.



The common SR's estimation model considers to establish a *trajectory* within the 3-dimensional space stretched by the three co-ordinates C1-C3 (see Fig. 1). Obviously in real life project such a trajectory is not a continued curve but is a piecewise linear one, because the development process represents decision making process

Fig. 1. The geometric understanding of subspace A

Then in order to analyze the whole SRA-trajectory we have to elaborate a method for estimation of belonging any given SRA to one of the areas:  $A^{(0)}$ ,  $A^{(1)}$ ,  $A^{(2)}$ ,  $A^{(3)}$ .

There are 4 bordered and qualitatively different areas of some SRA values, which are corresponding in subspace A to the points:  $a_1 = \sup(A^{(0)})$ ,  $a_2 = \inf(A^{(1)}) = \inf(A^{(2)})$ ,  $a_3 = \sup(A^{(2)})$  and  $a_4 = \sup(A^{(1)})$ .

Let's consider the new LV that is defined as:  $\beta_1 = \text{"Assessment of Current SRA"}$ . To solve our task a *membership function* (MF) for new LV should be determined. We can

additionally assume, that all three criteria C1, C2, C3 have the corresponding weight ratio, that defined as LV:  $\beta_2 =$  "Importance of SR's Criteria Assessment"; MF should be defined by experts. According to such admissions we can built the criteria assessments for different SRA values:  $a_1, a_2, a_3, a_4, a_c^{(k)}$  where:  $a_c^{(k)}$   $k = \overline{1,3}$  is some current SRA value.

Assessing of SRA  $a_1, a_2, a_3, a_4, a_c^{(k)}$  is defined by criteria C1, C2, C3, that are specified by the value of LV  $R_i^{(j)}$ , where:  $i$  - is a number of SRA to be estimated,  $j$  - is a number of criteria, according to which the SRA is estimated. The measure of criteria importance is defined by the value of LV  $W_j$ .

The weighted estimation of SRA  $a_i$  can be found by establishing of the left side  $a_i'$ , and the right side  $a_i''$  lower bottom of the MF-trapezium,  $a_i^*$  - the left side and  $a_i^{**}$  - the right side of upper bottom of the MF-trapezium. We receive these values using the following well-known formulas:

$$a_i' = \sum_{j=1}^3 W_j R_i'^{(j)}, a_i^* = \sum_{j=1}^3 W_j^* R_i^{* (j)}, a_i'' = \sum_{j=1}^3 W_j'' R_i''^{(j)}, a_i^{**} = \sum_{j=1}^3 W_j^{**} R_i^{** (j)}, \quad (1)$$

where:  $n$  - a total number of alternatives, for which the integral assessment is found. After that we define the new fuzzy set  $I$ , that is specified on the set of alternatives, and the value of the appropriate MF is interpreted as a characteristic of a measure how one SR's assessment (SRAS)  $a_i$  is better then SRAS of alternative  $a_4$ . This value is equal to the  $y$ -coordinate of an intersection of any alternative weighted, and the best alternative estimation  $a_4$ . And could be found by formula given in [DP88]

$$\mu_i = \sup_{x \geq y} \min (\mu_i(x), \mu_{a_4}(y)) \quad i = \overline{1,7} \quad x, y \in X^\Sigma. \quad (2)$$

The values  $\mu_i$  that have been received using (2), characterize the *distance* between any current SRA  $a_i$  from the state, where SRA is *not defined* (this is the area  $A^{(0)}$  on the Fig. 1). Hence, the values  $\mu_i$   $i = \overline{1,4}$  define the positions of border points:  $a_1, a_2, a_3, a_4$  on the new *universe set* for the LV introduced above: "Assessment of Current SRA" and used for the building the *new generalized MF* (see Fig. 2). It allows us for any current SRA to define it's location accordingly to the intervals which are corresponded with the areas  $A^{(0)}, A^{(1)}, A^{(2)}, A^{(3)}$  in the subspace  $A$  (see Fig. 1).

The elaborated approach for SR analyzing and management is supposed to make expertise of them more effectively.

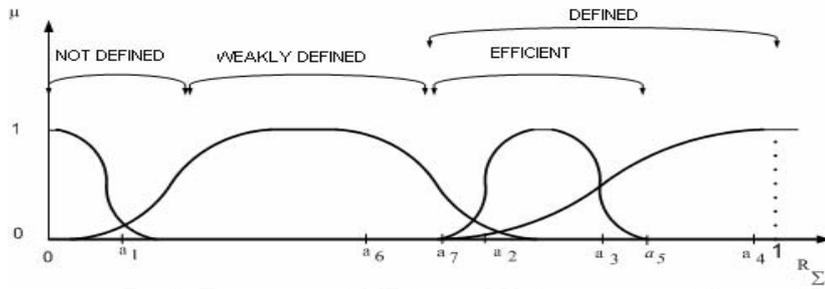


Fig. 2. The integrated MF for the LV: "Assessment of Current SRA"

## References

- [TSM04] Tkachuk M., Sokol V., Mayr H.C., et al. A Knowledge-based Approach to Traceability and Maintenance of Requirements for Information Systems // Problems of Programming.- Kiev. 2004. № 2-3 - pp.370 – 378.
- [DP88] Dubois, D., Prade, H. Theorie des Possibilites.- Masson. – Paris. - 1988